

QUANT      Maps Theory

Some Special Theory

RATIO THEORY

$$A:B = 2:3$$

$$B:C = 4:7$$

$$A_1:A_2 = 1:3 \checkmark$$

$$A_2:A_3 = 2:7 \checkmark$$

$$A_3:A_4 = 3:2 \checkmark$$

$$A_4:A_5 = 2:1 \checkmark$$

$$A_1 : A_2 : A_3 : A_4 : A_5 \text{ (in a single line)}$$

Rule

Multiply all the firsts  
One by one Ant last (last all Ant)

$$(1 \cdot 2 \cdot 3 \cdot 2) : (3 \cdot 2 \cdot 7 \cdot 7) : (3 \cdot 1 \cdot 7 \cdot 7) : (7 \cdot 1 \cdot 2 \cdot 2) : (3 \cdot 1 \cdot 7 \cdot 1)$$

2 : 6 : 3 : 2 : 1

1:3	2:3	3:4	1:2
A:B	B:C	C:D	D:E

$$(1/3 \cdot 2 \cdot 1) : (3/2 \cdot 3 \cdot 1) : (3 \cdot 3 \cdot 3 \cdot 1) : (3/3 \cdot 3 \cdot 4 \cdot 1) : (3 \cdot 3 \cdot 4 \cdot 2)$$

$$= 2 : 6 : 9 : 12 : 24$$

Topic: 2

HCF & LCM checked with trees of Ratio  
May come as a long problem...

- 1) Bell ringing together problem
- 2) Problem on working Schedules

Problem

- (i) Least number divisible  
LCM of a, b, c
- (ii) Least number which leaves  
remainders u, v, r → when divided by  
a, b, c

$$\frac{41}{10} \rightarrow \textcircled{i}$$

$$\frac{41}{15} \rightarrow \textcircled{ii}$$

$$\frac{41}{20} \rightarrow \textcircled{iii}$$

(ii) remainder  $a, v, r \rightarrow$  when divided by  $a, b, c$

$$(\text{LCM of } a, b, c) - K$$

$$\text{rem } K = (a - u) = (b - v) = (c - r)$$

Divided by  $\boxed{12, 16, 18}$  leaves a remainder  $\rightarrow$   $\textcircled{5}$   
 empty line

$$\frac{11}{2} \rightarrow \textcircled{1}$$

LCM of  $\left. \begin{array}{l} 12, 16, 18 \\ 2 \mid 2, 16, 18 \\ 2 \mid 1, 8, 9 \\ 2 \mid 1, 4, 3 \\ 2 \mid 1, 2, 3 \end{array} \right\} 144$

least number =  $\textcircled{144} + 5 = \textcircled{149}$

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$\textcircled{\text{iii}}$  Leaves NO remainder

LCM of  $a, b, c$

(Leave no of n digit + LCM - remainder)

$\rightarrow$  And we want perfect square which is divisible by  $2, 3, 4, 5, 6$

LCM  $\rightarrow$   $\textcircled{(2, 3, 4, 5, 6)}$   $\rightarrow$   $\textcircled{60}$

$$\sqrt{900} = 30$$

$60 \times 3 = 240, 720, 360$

$3 \cdot 5 \cdot 60 \Rightarrow 15 \cdot 60 = \textcircled{900}$

LCM  $\rightarrow$   $\textcircled{900}$

Least  $\rightarrow$  LCM } Times  
 Largest  $\rightarrow$  HCF }  $\leftarrow$

36, 42, 64 Largest number divisible

HCF of 36, 42, 64

$$\begin{array}{r} 36 \mid 12 \mid 1 \\ 42 \mid 14 \mid 1 \\ 64 \mid 16 \mid 1 \end{array}$$

$$\begin{array}{r} 6 \mid 57 \mid 5 \\ 57 \end{array}$$

LCF of 36, 42, 54

$$\begin{array}{r} 36 \times 12 \times 1 \\ \hline 36 \\ 6 \overline{) 36} \\ \underline{36} \\ 0 \end{array}$$

$$\begin{array}{r} 0 \overline{) 54} \\ \underline{54} \\ 0 \end{array}$$

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Answer: 2

$$36 = 2 \times 3 \times 3$$

$$54 = 2 \times 3 \times 3 \times 3 \rightarrow 2 \times 3 \Rightarrow 6$$

$$42 = 7 \times 2 \times 3$$

$$\frac{21}{4} \leftarrow 1$$

Double Remainder Problem

If divided by 575 Remainder  $\rightarrow 5$   
 ~ ~ 386 ~ ~  $\rightarrow 6$

$$575 - 5 = 570 \text{ Double}$$

$$386 - 6 = 380$$

190 is the HCF

HCF  $\frac{190}{570, 380}$   
 $\frac{3}{2}$

# Find the least number which divides 93, 131, 188  $\rightarrow$  leaving the same remainder...

# Time intervals Band numbers

Remainder  $\rightarrow r$

$$93 - r, 131 - r, 188 - r$$

$(2-1) \& (3-2)$

Take 2 @ a time ..

$$(131 - r) - (93 - r) \& (188 - r) - (131 - r)$$

$$(131-r) - (93-r) \times (180-r) \dots$$

$$\rightarrow (38) \quad (57)$$

$$\text{HCF } 38, 57 \rightarrow (19)$$

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## Time Interval Problem

# 6 bells ring @ intervals. 2, 4, 6, 8, 10, 12 seconds.  
They started ringing simultaneously. In (30 min) how many times they ring together?

$$\text{LCM } 2, 4, 6, 8, 10, 12 \rightarrow (120)$$

$$2 \text{ min } \left( \frac{30}{2} + 1 \right) \rightarrow 16$$

$$\left( \frac{30}{a} + 1 \right) \rightarrow \text{LCM of intervals} \dots$$

## # Percentage Short cut System

$$70 \rightarrow 20\% \uparrow \rightarrow 70 \times 1.2 \quad (1+0.2)$$

$$30\% \downarrow \rightarrow 70 \times 0.7 \quad (1-0.3)$$

$$70 \rightarrow 35\% \uparrow \rightarrow 70 \times 1.35$$

$$39\% \downarrow \rightarrow 70 \times (0.61)$$

## Multiple times percentage change

$$100 \quad 10\% \uparrow \quad 20\% \uparrow \quad 15\% \uparrow \quad 20\% \downarrow \quad 15\% \downarrow$$

$$100 \rightarrow 100 \times 1.1 \times 1.2 \times 1.15 \times 0.8 \times 0.85$$

to do same it 5 times

100 → 100 × 1.1 × 1.2 × 1.15 × 0.8 × 0.85  
 13.25% no need to change it 5 times..

# A value changes 7 times  
 find % change of the value ???  
 (100 → 200) 100% 60%

1 ten times = %

400 → 29.312% ↑

400 → 1.29312

- 10.00
- 10% → 1.10
- 22 → 1.22
- 01% → 1.01
- 01.237 → 1.0123
- 05% → 1.05

01.37% ↑  
 100 × 1.0137

1.345% ↓  
 100.01345

9062395723

75  
 1.15  
 1.01

1.000000  
 0.01345  
0.98655

Under home list meaning

Self Host / 60

200 → 60

