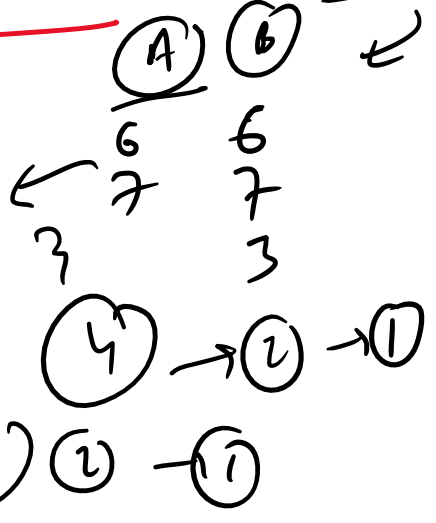


The word of Distribution

Random. 2023/2019 Word up

2011 2015

- 1
 - 2
 - 3
 - 7
 - 5 - - -
- 1 → 2
1 → 3



Main idea of this distribution

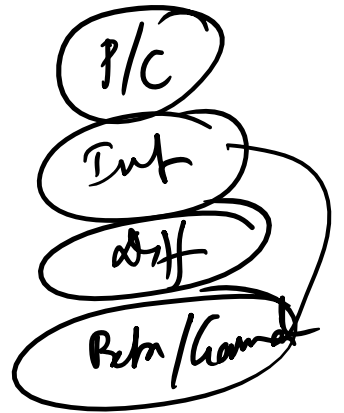
32

8 steps

9062395123



10



How many matches ..

- 1 → 2
- 1 → 3
- 1 → 4
- 1 → 9

$$9 + 8 + 7 + 6 + 5 + 4 + 3 + 2 + 1$$

$$\Rightarrow \frac{9 \cdot 10}{2} \Rightarrow 45$$

+2
+1
28

$$\Rightarrow B(n, p) \ll$$

B/P/N / 4/5B



|| | odd ??

Binomial \rightarrow Hard odd??
 n times

$$X \sim B\left(n, p = \frac{1}{2}\right)$$

$$p(x) = nC_x \left(\frac{1}{2}\right)^x \left(\frac{1}{2}\right)^{n-x}$$

$$= nC_x \left(\frac{1}{2}\right)^n \quad x = 0, 1, 2, \dots, n$$

$$p_1 = p(1) + p(3) + p(5) + \dots$$

$$= \left(\frac{1}{2}\right)^n [nC_1 + nC_3 + nC_5 + \dots]$$

$$= \left(\frac{1}{2}\right)^n [2^n - 1] = \frac{1}{2}$$

Ans

$$nC_1 + nC_2 + \dots + nC_n = 2^n - 1$$

$$nC_0 + nC_1 + \dots + nC_n = 2^n$$

BD vs NBD

10mg
2sun

Total time travel

4 Sues
35

Sues is freed...

14th Feb \rightarrow 2

15/2

Th Fri Sat
 (C.A. Route)

Sub Finite

Necessary vs Sufficient Cond.

a, b

$a > b > 0$
 ↑ ↓
 true val.

Necessary

$a = np > 0$ $n > 0 \quad b > 0$
 $b = nq > 0$ $n > 0 \quad b > 0 \quad q > 0$
 $0 < b, q < 1$ $a, b > 0$

$\frac{a^2}{a-b}$

$= \frac{n^2 p^2}{np - nq} = \frac{n^2 p^2}{np(1-q)} = \frac{n^2 p^2}{np^2} = n$
integer

Suffice

$a > b > 0$

$\frac{a^2}{a-b} \Rightarrow$ integer
 det, $b = af$
 $0 < f < 1$

$n = \frac{a^2}{a-b} = \frac{a^2}{a-af}$
 $n = \frac{a}{1-f}$

$a = n(1-f)$

$b = af = n(1-f)f$
 $0 < f < 1$

$$\text{Any } f = q \quad (0 < q < 1)$$

$$1 - f = 1 - q = p$$

$$a = n(1 - f) = np$$

$$b = nt(1 - f) = npq$$

$X \rightarrow$ r.v. prob function $\rightarrow b$

\rightarrow let, $Y = \frac{X}{n}$ be a random variable $\binom{x; n, p}$

$$E(Y), v(Y) = ??$$

if $p(y) = ??$ where $p(y)$ is a prob function..

$$X \sim b(x, n, p) \quad f(x) = \binom{n}{x} p^x q^{n-x}$$

$x = 0, 1, 2, 3, \dots, n$

$$E(X) = np \quad v(X) = npq$$

$$Y = \frac{X}{n} \quad E(Y) = E\left(\frac{X}{n}\right) = \frac{1}{n} E(X) = \frac{np}{n} = p$$

$$v(Y) = \text{var}\left(\frac{X}{n}\right) = \frac{1}{n^2} npq = \frac{pq}{n}$$

The distribution function $F(y)$ of Y

$$F_Y(y) = P(Y \leq y) = P\left(\frac{X}{n} \leq y\right) = P(X \leq ny)$$

$$= \dots + f(n-1) + f(n)$$

$$\Rightarrow P_Y(y) = f(0) + f(1) + f(2) + \dots + f[n(y-1)] + f(ny)$$

Now, $P_Y(y-1) = P(Y \leq y-1)$
 $= P[X \leq n(y-1)]$
 $= f(0) + f(1) + \dots + f[n(y-1)]$

\therefore (PMF) $\rightarrow p(y) = P(y) - P(y-1)$
 $= f(ny) = {}^n C_{ny} p^{ny} q^{n-ny}$

Possible vals $\cdot 0, \frac{1}{n}, \frac{2}{n}, \dots, 1$

$X \sim B(n, p)$

$E\left[\frac{1}{1+X}\right] = ?$

$$\sum_{x=0}^n \left(\frac{1}{1+x}\right) {}^n C_x p^x q^{n-x} = \sum_{x=0}^n \left[\frac{n!}{x!(n-x)!} \cdot \frac{p^x q^{n-x}}{(x+1)} \right]$$

$$= \sum_{x=0}^n \left[\frac{(n+1)!}{(x+1)!(n-x)!} \cdot \frac{p^{x+1} q^{n-x}}{(n+1)p} \right]$$

$$= \frac{1}{(n+1)p} \sum_{x=0}^n {}^{n+1} C_{x+1} p^{x+1} q^{(n+1)-(x+1)}$$

$\cdot \dots \cdot n+1-1 \quad n+1-1 \quad \dots \quad 2 \quad (n+1)-2$

$$\begin{aligned}
 &= \frac{1}{(n+1)p} \sum_{n=0}^{\infty} \left[\binom{n+1}{1} b q^{n+1-1} + \binom{n+1}{2} b^2 q^{2(n+1)-2} \right. \\
 &\quad \left. + \dots + \binom{n+1}{n+1} b^{n+1} q^0 \right] \\
 &= \frac{1}{(n+1)p} \left[(q+b)^{n+1} - \binom{n+1}{0} q^{n+1} \right] \\
 &= \frac{1 - q^{n+1}}{(n+1)p}
 \end{aligned}$$

HW $E \left[(1+x)^{-1} (2+x)^{-1} \right]$



Ryuler Die

$(7) \quad (21)$
 $6+5+4+3+2+1$
 $\Rightarrow (21)$

Prize on 7th success

He needs to draw 5 or 6

He needs to draw total no of throws

$p \Rightarrow 5 \text{ or } 6 = \frac{2}{6} = \frac{1}{3}$

~~$P(\text{win}) = \sum_{k=1}^{\infty} k \cdot \left(\frac{1}{3}\right)^k \cdot \left(\frac{2}{3}\right)^{k-1}$~~

draw $(n) \rightarrow$ So that mod = 7

denote $(n) \rightarrow$ some

Let, $(n+1) \equiv \frac{n+1}{3} \pmod{K}$ (integer)

then $BD \rightarrow$ BT-model

mod $K, K-1$

$$K-1 \leq \text{mod} \leq K$$

need to find n in a way

$$\text{So, } \frac{n+1}{3} - 1 \leq 7 \leq \frac{n+1}{3}$$

$$\frac{n-2}{3} \leq 7 \leq \frac{n+1}{3}$$

Front part

$$n \leq 23$$

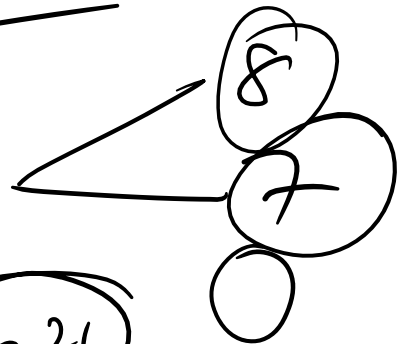
Second part

$$20 \leq n$$

$$20 \leq n \leq 23$$

$$n = 21, 22, 23$$

@ $n=23$, $(n+1) \equiv \frac{24}{3} \equiv 8$



$$n = 21, 22$$

$$n = 21$$

