

Growth Model

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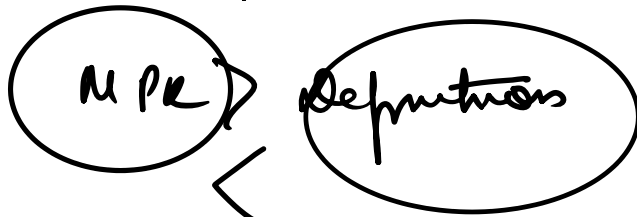
Golden Rule

Till which point we will proceed

Depreciation = MPK

Create something new → Cost (100)

Depreciation → (100)



(L)
Labour

(LE)

Effective Labour

$\epsilon \rightarrow$ efficiency factor of the labour

#

Cobb Douglas Production function

$$Y = K^\alpha (\bar{L}E)^{1-\alpha}$$

$\alpha = 1/3$

$L = 100 \quad K = 40 \quad \bar{E} = 50$

a) Potential output per worker??

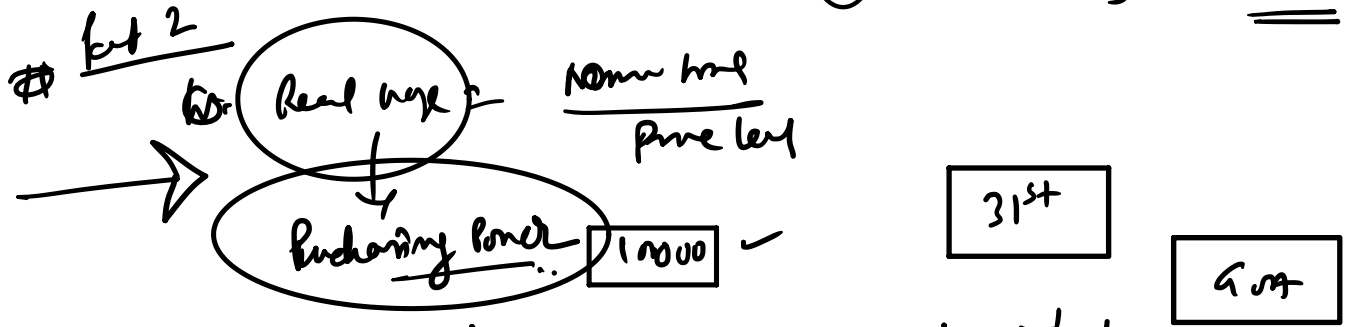
b) market clearing Real wage rate [@ full employment]

$$Y = K^\alpha (\bar{L}E)^{1-\alpha}$$

$$y = \frac{Y}{\bar{L}E} = \left(\frac{K}{\bar{L}E}\right)^\alpha = \left(\frac{40}{100 \times 50}\right)^{1/3} = \left(\frac{1}{5}\right)$$

$$y = \frac{Y}{LE} = \left(\frac{K}{LE}\right)^\alpha = \left(\frac{100}{10 \times 50}\right)^{\frac{1}{3}} = \left(\frac{1}{5}\right)$$

Potential output/wage = $(y) \times (LE) = \frac{1}{5} \times 50 = \underline{\underline{10}}$

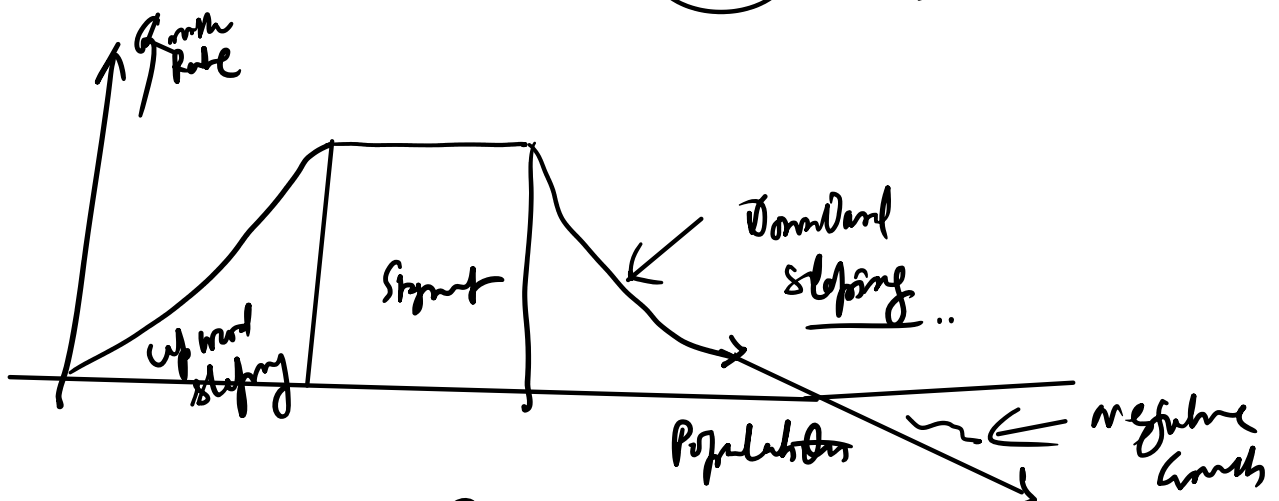
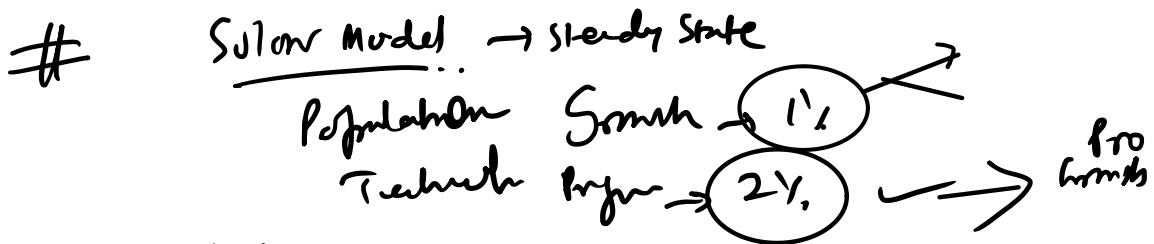


$$MPK = \frac{dy}{dK} = \alpha K^{\alpha-1} = \frac{1}{3} \left(\frac{1}{125}\right)^{\frac{1}{3}-1} = \frac{1}{3} \left(\frac{1}{125}\right)^{-\frac{2}{3}}$$

$$= \frac{1}{3} = \frac{25}{3} = 8.33$$

$w = 8.33$

(a) MPK the wage Rate is exactly market clearing



Output & K grow @ 3%.
K share of Y is 0.3.

Population → negative growth zone

$Y = f(K, L, A)$ (TP)

$\frac{dY}{Y} = \alpha \frac{dK}{K} + (1-\alpha) \frac{dL}{L} + \frac{dA}{A}$

change → $\frac{dY}{Y}$
Rise value → $\frac{dY}{Y}$

α = share of K
 $(1-\alpha)$ = share of L

$3Y = 0.3(3\%) + 0.7(1\%) + 2\%$

Income dA

Steady state
distribution
Spent dA

$6.30 - 7.30$

2023 ↑

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Q $Y = \sqrt{LK}$

$nK = 0.8$

$d = 10\%$ of Capital

Population → 2%/year

- (i) Calculate steady state value of PCO & Consumption/Capita
- (ii) Find savings rate & $\frac{K}{L}$ ratio which max Consumption/Capita.

Ans.

Break Even level → $(\frac{f}{n})K$

Savings → $s f(K)$

$Y = \sqrt{LK}$
 $Y = \sqrt{K}$

Savings $\Rightarrow \delta f(k)$

$$Y = \sqrt{KL}$$
$$\frac{Y}{L} = \sqrt{\frac{K}{L}} = y$$
$$y = \sqrt{K}$$

ans, $\delta = \text{MPS} = \text{APS} = 1 - \text{MPC} = \underline{0.2}$

$$f(k) = \sqrt{k}$$

find Solow Growth model

$$\theta \cdot \delta f(k) = (\delta + n)k$$

$$0.2 k^{\frac{1}{2}} = (0.1 + 0.02) k$$

$$\sqrt{k} = \frac{0.20}{0.12} = \frac{5}{3} = \textcircled{1.67}$$

$$k = \underline{\underline{2.78}}$$

for map Consumption / Capita..

$$\delta f(k) = (\delta + n)k$$

$$0.2 \times k^{\frac{1}{2}} = c$$

Part 2

Golden rule steady state

$$MP_k = (\delta + n)$$

$$y = \sqrt{k}$$

$$\frac{dy}{dk} \Rightarrow$$

$$\frac{1}{2} k^{-\frac{1}{2}} = 0.12$$

$$k^{\frac{1}{2}} = \frac{1}{2(0.12)} = \frac{1}{0.24}$$

$$\Rightarrow k = \boxed{17.36}$$

Again, $\delta K^{\frac{1}{2}} = (\delta + n) K^{\frac{1}{2}}$

$$\delta = \frac{(0.1 + 0.02)}{2(0.1 + 0.02)} = \frac{1}{2}$$

$$\delta = 0.5$$

Production function $\rightarrow \frac{Y}{L}$ or y

2014

$$Y = A K^{0.5} L^{0.5}$$

$$\frac{Y}{L} = A \left(\frac{K}{L}\right)^{0.5}$$

$$y = A \sqrt{k}$$



Per capita formation ..

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$$Y_t = Y_{t-1}$$

$$Y_t = f(Y_{t-\tau})$$

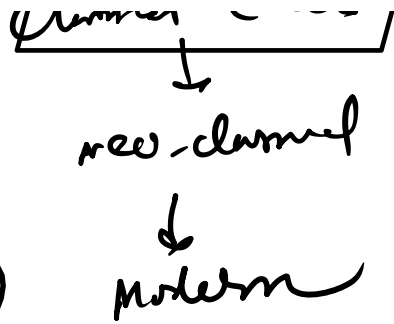
$$\tau \in \mathbb{N}$$

Unusual cases

\downarrow

$$n \geq 30 \text{ large } \mathbb{N}$$

$$n < 30 \text{ (1)}$$



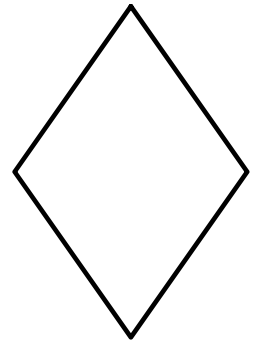
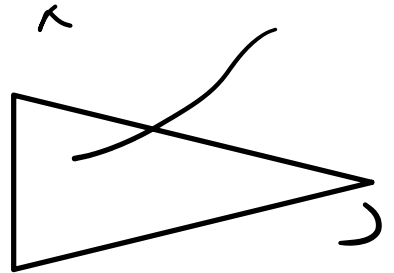
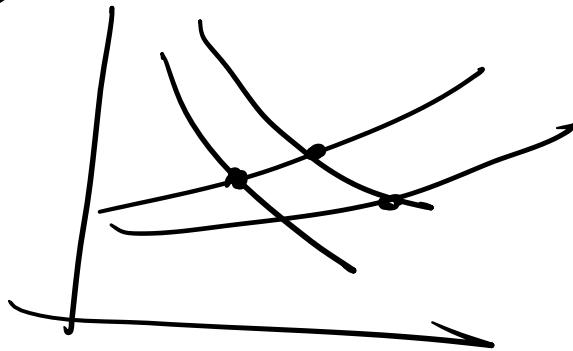
$n \geq 30$ $\text{deng}(N)$
 $n < 30$ (t)

(IFS)

$n \times$

The per Capita K share $\Rightarrow \left(\frac{K}{L}\right)$ grows over time
 with an increase in Y/L as economy moves from one
 steady state to another.

When smaller
 steps function
 @ that point
 we can have
Equilibrium



For $y = \frac{Y}{L}$

$$\ln y = \ln Y - \ln L$$

$$\frac{1}{y} \frac{dy}{dt} = \frac{1}{Y} \frac{dY}{dt} - \left(\frac{1}{L} \frac{dL}{dt} \right) \rightarrow 0 \text{ as } n \rightarrow 0$$

$$\frac{1}{y} \frac{dy}{dt} = \frac{1}{Y} \frac{dY}{dt}$$

Population dynamics